Three-dimensional organ extraction method for color volume image based on the closed-form solution strategy

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**Background:** With the rapid development of computer technology, surgical training, and the digitalized teaching of human body morphology are gaining prominence in medical education. Accurate, true organ models are essential digital material for these computer-assisted systems. However, no direct three-dimensional (3D) true organ model acquisition method currently exists. Thus, the direct extraction of the interested organ models based on the existing Virtual Human Project (VHP) image set is urgently needed.

**Methods:** In this paper, a closed-form solution-based volume matting method is proposed. Using a small quantity of graffiti in the foreground and background, target 3D regions can be extracted by closed-form solution computing. The upper triangular storage strategy and the preconditioned conjugate-gradient (PCG) method also promote robustness.

**Results:** Four image data sets (2 virtual human male and 2 virtual human female) from the United States National Library of Medicine (including brain slices, eye slices, lung slices, heart slices, liver slices, kidney slices, spine slices, arm slices, vastus slices, and foot slices) were selected to extract the 3D volume organ models. The experimental results show that the extracted 3D organs were acceptable and satisfactory.

**Conclusions:** This method may provide technical support for medical and other scientific research fields.

**Keywords:** Virtual Human Project (VHP); color volume image; image matting; closed-form solution


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Introduction

The Virtual Human Project (VHP) was founded by the United States National Library of Medicine (NLM). As the first research stage, the visualization of virtual human data has extraordinary significance. It has broad application prospects in medical research and clinical education: surgical training, prosthetic modeling, and digitalized teaching of human body morphology. The foundation and application for this research rely on the acquisition of accurate three-dimensional (3D) models of VHP organs. Therefore, extracting the organs from the massive VHP 3D image database has become an urgent need. At present, the most commonly used approach is manually extracting regions of interest in serialized slice images. Obviously, the efficiency of this procedure (slice-by-slice processing) is very low. For computing, the most direct approach is segmenting the VHP images with the matting method. However, existing methods are also two-dimensional (2D)-image-oriented (slice-by-slice processing). In addition, it is common for sudden changes to occur between the extracted regions in adjacent slice images. Another potential method is machine learning-based strategy. However, because of its heavy reliance on the training model, the machine learning...
strategy is mainly suitable for large scale image data but not suitable for single image data (such as VHP image data). Therefore, it is essential to design an approach for the direct segmentation of the VHP 3D volume image.

Here, we propose a 3D organ extraction method for color volume image based on the closed-form solution strategy. In this method, to address the massive coefficient matrix processing, we designed an upper triangular storage strategy to store the considerable data and used the preconditioned conjugate-gradient (PCG) method to solve the linear equation. This method only needs to mark the target region and non-target region with manual markings to directly extract the 3D organs.

**Literature review**

Image matting is a classic research topic and mainly focuses on obtaining the region of interest (ROI) in the image. Several outstanding methods have been proposed to solve this issue. Levin et al. presented a closed-form solution to natural image matting (1). High-quality mattes for natural images may be obtained from a small quantity of user input. Yan et al. presented a correlation-based sampling method in which the image pixel correlation is employed in color sampling (2). Cai et al. proposed a cooperative coevolution differential evolution (DE) algorithm to improve the efficiency of searching for high-quality sample pairs (3), and other studies have used a similar method (4-7). Johnson et al. conceived the matting problem as a sparse coding of pixel features (8). Cho et al. presented an image matting algorithm to extract consistent alpha mattes across sub-images of a light field image (9). Several other similar methods (10-13) also achieved a satisfactory effect.

In addition to geometrical and mathematical means, some matting methods use learning to achieve their results. Chen et al. proposed a deep learning framework (called TOM-Net) to learn the refractive flow (14). He et al. proposed an approach with RGB-Depth (RGB-D) data based on iterative transductive learning (15). They also presented a new method to form the Laplacian matrix in transductive learning. Xu et al. proposed a deep image matting method (16) that could address 2 issues: (I) the use of only low-level features and (II) the lack of high-level context. Zou et al. introduced a method of video matting via sparse and low-rank representation (17). Other studies (18-20) have implemented similar research methods.

Matting methods have not yet been extensively applied in medical imaging. This may be due to the fact that matting methods are more suitable for multi-channel color image segmentation rather than single-channel gray level image segmentation. There have been a few typical related studies in recent years. Cheng et al. worked on improving the matting algorithm by adding a weight extension and referred to this as adaptive weight matting (AWM) (21). Li et al. proposed a new end-to-end iterative network for tongue image matting, which directly learns the alpha matte from the input image by correcting any misunderstandings in intermediate steps (22). Fan et al. proposed a hierarchical image matting model, where a hierarchical strategy is integrated to extract blood vessels from fundus images (23). Several other methods have also been designed and tested for different medical image processing applications (24-27).

From a review of the existing methods, we can see that all strategies, including common matting methods, learning-based methods, medical image-oriented methods, are designed and suitable for 2D images. How to directly extract target organs from 3D volume images by matting strategy is thus an interesting and challenging issue.

**Methods**

From the above methods, we can see that all the published literature centers around 2D image matting. However, there has not been a matting method developed thus far for 3D volume images. Here, we propose a closed-form solution-based volume matting (CFSVM) method for the VHP 3D volume image dataset. The main flow chart of the 3D volume image data matting in this paper is shown in Figure 1.

**Volume image construction of VHP slices**

The VHP image dataset is composed of a large number of serialized slice images. Our goal is to directly extract the target 3D organ from an original 3D volume image dataset. Therefore, the first step in reconstructing the volume image by the serialized 2D slice images (as shown in Figure 2).

**Markings for foreground and background**

To obtain the 3D ROI from the constructed 3D volume image, it is necessary to mark the foreground (target) and the background (nontarget) in the 3D volume image. In our method, a brush is used to manually mark the foreground markings and background markings on a certain layer of the 3D volume image (as shown in Figure 3). Meanwhile,
the coordinates of the markings path and its corresponding voxel values are recorded in different vectors.

**3D ROI extraction from the 3D volume image**

For image matting, we can consider an image as a linear combination of its foreground image and its background image. In our method, by referencing 2D image segmentation methods (28), this linear combination for a 3D volume image can be presented as the following:

\[ V = \alpha F + (1 - \alpha) B \]  \hspace{1cm} [1]

where \( V \) is the 3D volume image, \( \alpha \) is the transparency of the foreground image, \( F \) represents the foreground voxels, and \( B \) represents the background voxels. Then, the deformation of the formula can be obtained as follows:

\[ \alpha = \frac{V - B}{F - B} = \frac{1}{F - B} V + \left( \frac{B}{F - B} \right) \] \hspace{1cm} [2]

A known 3D volume image \( V \) is the summation of the foreground \( F \) and background \( B \). Thus, \( \alpha \) is obtained; the foreground (ROI) \( F \) can be calculated. Here, we utilize the value of local \( \alpha_i \) to estimate the value of \( \alpha_g \) for the whole volume image. Then, the 3D ROI in the volume image can be extracted. The specific steps are outlined below.

**\(\alpha_g\) computation by closed-form solution strategy**

Similar to the formula above [1], we can obtain the linear formula of the \( i \)-th voxel in a locally small window (3×3×3 voxels in our method):

\[ V_i = \alpha_i F_i + (1 - \alpha_i) B_i, \forall i \in w \] \hspace{1cm} [3]

where \( V_i \) is the \( i \)-th voxel, \( F_i \) and \( B_i \) are the \( i \)-th voxel’s foreground and background, and \( \alpha_i \) is the \( i \)-th voxel’s opacity of the foreground. Referencing the second formula [2], a formula transformation can be obtained from the third formula [3]:

\[ \alpha_i = aV_i + b \forall i \in w \] \hspace{1cm} [4]

where \( a = \frac{1}{F - B}, b = \frac{B}{F - B} \). To obtain the value of \( \alpha_g \) for the whole volume image, an energy function (1) is utilized. The \( \alpha_g \) value can be calculated by minimizing the energy

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Figure 1 Flow chart of 3D volume image matting. VHP, Virtual Human Project.

Figure 2 3D volume image reconstruction from serialized slice images.
function as follows:

$$J(\alpha, a, b) = \sum_{i,j} (\alpha_i - a_i V_i - b_i)^2 + \epsilon a_i^2$$

[5]

where $W_i$ is a small window around voxel $k$, and $\epsilon a_i^2$ is a regular term to maintain the stability of the values in the window. According to the deformation and derivation of the energy function, we can obtain the following:

$$J(\alpha_g) = \alpha_g^T L \alpha_g$$

[6]

where $L$ is an $N\times N$ matrix whose $(i,j)$-th element is

$$L(i,j) = \sum_{k,l} \left[ \delta_{ij} - \frac{1}{|W_k|} \left( 1 + \frac{k^2}{|W_k|} \right) \left( V_i - \mu_i \right) \left( V_j - \mu_j \right) \right]$$

[7]

where $\mu$ is a covariance matrix, $\mu_k$ is the color mean vector in a small window $W_k$, $V_i$ is an identity matrix, $V_i$ and $V_j$ represent values of the $i$-th and $j$-th voxels, and $\delta_{ij}$ is the Kronecker delta.

To match the extracted $\alpha_g$ with the handmade graffiti, we can solve the following formula:

$$\alpha_g = \arg \min_{\alpha} \alpha_g^T L \alpha_g + \lambda (\alpha_g^T - d^T) D (\alpha_g - d)$$

[8]

where $\lambda$ is a constant (100 in our method), $d$ is a vector that is composed of the specified $\alpha_g$ values for voxels in the graffiti and 0 for other voxels, $D$ is a diagonal matrix whose diagonal elements are 1 for voxels in the markings and 0 for other voxels. To obtain the minimum value in the eighth formula [8], we need to set only its derivatives to 0. Thus, the following formula can be derived:

$$(L + \lambda D)\alpha_g = \lambda d$$

[9]

All variables are known in the final formula [9], so by solving sparse linear equations, we can obtain the value of $\alpha_g$.

**Voxel traversal in the volume image**

In the process of solving the energy function, we need to traverse all the voxels in the 3D volume image. This process contains two steps: (I) small windows (3×3×3 voxels) traversal in the entire 3D volume image and (II) all voxels traversal in each small window. This procedure is shown in Figure 4.

**Storage and solution for computational matrix**

In the process of solving the energy function [5], we found that the obtained intermediate data were sparse, which means that the number of nonzero elements was relatively small. For a simpler and more convenient computation when the matrix is inverted in solving linear equations, a storage method of the sparse matrix was designed. In this design, the coordinates of nonzero elements and their values are mainly stored. For a large-scale 3D sparse matrix, there may be memory abnormalities in solving linear equations. Because the sparse matrix is symmetric, positive, and definite, we propose a space-saving strategy. In our method, the upper triangle storage format is utilized for matting storage. Meanwhile, the stored data are accessed many
times until all of the data in the sparse matrix are traversed. After all the computational results are stored in the original storage format in the sparse matrix, we can obtain the solution of the linear equations. Assuming that the storage form of the matrix is shown in the left part of Figure 5 (the matrix has $n$ rows and $n$ columns, and $y$ represent values of some nonzero elements), the right part is its form of an upper triangular matrix. This storage method ensures that memory abnormalities can be avoided.

In the process of solving equation [9], the processing speed is also very important. In mathematics, preconditioned conjugate gradient (PCG) is a fast and effective method for solving a large linear sparse equation $Ax = B$ (where $A$ is a $N \times N$ matrix, $B$ is a $N \times 1$ vector, $x$ is unknown). It has the advantage of a fast convergence rate and small storage. In the PCG method, residuals and margins are used to search the solution of linear equations. Using this method, we can obtain the following:

\[
\begin{cases}
    r_{k+1} = c - Bx_{k+1} \\
    z_{k+1} = r_{k+1} - \frac{(r_{k+1}, Bz_k)}{(z_k, Bz_k)} z_k = r_{k+1} + \frac{||r_{k+1}||^2}{||z_k||^2} z_k
\end{cases}
\]  

[10]

where $B = M^{-1} A$, $c = Bx$, $M$ is the matrix preprocessed in the conjugate gradient method, $r_{k+1}$ is the residue after $k+1$ times iteration, $Z_{k+1}$ is the conjugate direction after $k+1$ times iteration, and $x_{k+1}$ is the solution after $k+1$ times iteration. The iteration times should not be larger than matrix order $N$.

**ROI extraction in the volume image**

By the obtaining $\alpha_{g}$, we can construct a mask image in the following way:
\[ \text{mask} = (\alpha_g \geq \alpha_{gT_{\text{min}}}) \odot (\alpha_g \leq \alpha_{gT_{\text{max}}}) \quad [11] \]

where \( \odot \) is a dot product operation, \( \alpha_{gT_{\text{min}}} \) is the minimum threshold of \( \alpha_g \), \( \alpha_{gT_{\text{max}}} \) is the maximum threshold of \( \alpha_g \), \( (\alpha_g \geq \alpha_{gT_{\text{min}}}) \) represents that all the elements in \( \alpha_g \) that are not less than \( \alpha_{gT_{\text{min}}} \) are set to 1 (and are otherwise set to 0), \( (\alpha_g < \alpha_{gT_{\text{max}}}) \) means that all the elements in \( \alpha_g \) that are not greater than \( \alpha_{gT_{\text{max}}} \) are set to 1 (and are otherwise set to 0). In our method, when the maximum and minimum thresholds are 0.2 and 0.9, the mask image is better. Under this condition, the ROI can be extracted by solving the formula representing the target 3D ROI: \( V_{\text{ROI}} = V \odot \text{mask} \cdot V_{\text{ROI}} \).

**Experiments and results**

In this paper, the VHP slices were utilized as 3D volume experimental images to test our method. The image data sets were collected by the United States National Library of Medicine and the Southern Medical University of China. There were 4 image data sets available (2 virtual human male and 2 virtual human female). Other image data set information was as follows: digit capacity, 24 bits color; interlayer spacing, 2 mm for U.S. Virtual Human and 0.2 mm for Chinese Virtual Human. Our method was implemented by the C++ language (Microsoft Visual Studio). The hardware parameters were the following: CPU, 1.90 GHz, memory, 4 GB. Several typical organ slices (including brain slices, eye slices, lung slices, heart slices, liver slices, kidney slices, spine slices, arm slices, vastus slices, and foot slices) were selected to extract the 3D volume organ models. The original slice images and the extracted 3D volume organs are shown in Figure 6. Our method could segment the ROI organs directly from the original 3D volume image. The 3D organs obtained were acceptable and satisfactory. Some local tiny organ details could also be accurately extracted, such as those of the central cerebral sulcus, leg vessels, pupil, and cardiac aorta.

For the experimental result assessment, there is presently no common indicator or benchmark, but one commonly used means is visual assessment. In our experiment, we invited the professional anatomical physician of the Dalian Medical University of China to evaluate the experimental results, and the assessment feedback was positive.

**Conclusions**

In the traditional means for segmenting the organ regions in the VHP image dataset, we usually utilize software (e.g., Photoshop) to manually extract the ROIs slice by slice, which is a very tedious job. To promote other related research (e.g., computer-assisted surgery), there is an urgent need for direct organ extraction from the VHP original volume image data. However, no such method currently exists.

In this paper, a CFSVM method is proposed to extract the organs of interest in the VHP volume image data. This volume image matting method has the advantage of good interaction and limited input requirements from users. We only need to mark (manual markings) the ROI (foreground) and region of noninterest (background) in the volume image to obtain the target organs. In the experiment, the greatest difficulty was the volume of data processed. The colors of different human organs are very similar. Thus, completing massive coefficient matrix processing is a challenging issue. We designed an upper triangular storage strategy to store the considerable data and use the PCG method to solve the linear equation. Thus, the processing procedure was made more robust. The extraction results show the effectiveness of our CFSVM method. In the future, this method may
Figure 6

Original VHP slice images and extracted 3D organs. VHP, Virtual Human Project.
have more applications in medical and other scientific research fields.

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Footnote

Conflicts of Interest: All authors have completed the ICMJE uniform disclosure form. The authors have no conflicts of interest to declare.

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