



Voxel-wise Optimization of Pseudo Voigt Profile (VOPVP) for Z-spectra fitting in chemical exchange saturation transfer (CEST) MRI

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Background: Chemical exchange saturation transfer (CEST) MRI is a promising approach for detecting biochemical alterations in cancers and neurological diseases, but the quantification can be challenging. Among numerous quantification methods, Lorentzian difference (LD) is relatively simple and widely used, which employs Lorentzian line-shape as a reference to describe the direct saturation (DS) of water and takes account of difference against experimental CEST spectra data. However, LD often overestimates CEST and nuclear overhauser enhancement (NOE) effects. Specifically, for fast-exchanging CEST species require higher saturation power (B_{1_sat}) or in the presence of strong magnetization transfer (MT) contrast, Z-spectrum appears more like a Gaussian line-shape rather than a Lorentzian line-shape.

Methods: To improve the conventional LD analysis, the present study developed and validated a novel fitting algorithm through a linear combination of Gaussian and Lorentzian function as the reference spectra, namely, Voxel-wise Optimization of Pseudo Voigt Profile (VOPVP). The experimental Z-spectra were pre-fitted with Gaussian and Lorentzian method independently, in order to determine Lorentzian proportionality coefficient (a). To further compensate for the line-shape changes under different B_{1_sat} 's, a B_1 -dependent adjustment was applied to the experimental Z-spectra (Z_{exp}) according to the prior knowledge learned from 5-pool Bloch equation-based simulations at a range of B_{1_sat} 's. Then, the obtained Z-spectra (Z_{B1adj}) was fitted by the previously defined VOPVP function. Considering the asymmetric component of MT, the positive- and negative-side of Z-spectra were fitted separately, while the middle part (-0.6 to 0.6 ppm, consisted primarily of DS) was fitted using Lorentzian function. Finally, the difference between Z_{VOPVP} and Z_{exp} was defined as the CEST and NOE contrast. To validate our VOPVP method, an extensive simulation of CEST Z-spectra was performed using 5-pool model and 6-pool model with greater MT component.

Results: In comparison with LD approach, VOPVP exhibited lower sum of squares due to error (SSE) and higher goodness of fit (R-square) for the experimental Z-spectra at all B_{1_sat} . Moreover, the results indicated that VOPVP fitting improved the overestimated contributions from amide proton transfer (APT) and NOE through LD at all B_{1_sat} . Despite that the relationship for B_1 -dependent adjustment was pre-determined using a single 5-pool model, the VOPVP fittings obtained accurate quantification for multiple 6-pool models with a range of T_1 's and T_2 's. The robustness of VOPVP fitting was also proved by simulations using 3T parameters. Furthermore, we assessed VOPVP *in vivo* in a glioblastoma-bearing mouse. Compared to LD maps, VOPVP quantification maps displayed higher contrast-to-noise ratio between tumor and normal contralateral tissue for APT, glutamate and nuclear overhauser effect (NOE), when $B_{1_sat} > 1 \mu T$.

Conclusions: As an improvement of LD method, VOPVP fitting can serve as a simple, robust and more accurate approach for quantifying CEST and NOE contrast.

Keywords: Chemical exchange saturation transfer (CEST); Lorentzian fit; amide proton transfer (APT); nuclear overhauser enhancement (NOE); Pseudo Voigt profile

Submitted Jul 16, 2019. Accepted for publication Sep 29, 2019.

doi: 10.21037/qims.2019.10.01

View this article at: <http://dx.doi.org/10.21037/qims.2019.10.01>

Introduction

Chemical exchange saturation transfer (CEST) is a magnetic resonance imaging (MRI) technique for detecting low-concentration metabolites and molecules with exchangeable protons at specific resonance frequencies, which can be labeled by a saturation pulse allowing signal transfer to water pool for detection (1-3). CEST MRI (1,4) has been applied to detect exogenous or endogenous amine (5), amide (6), creatine (7), glucose (8,9), glutamate (10), glycogen (11) and glycosaminoglycan (12). Additionally, CEST technique can probe the micro-environment of tissue, including temperature (13) and pH (14,15). These unique capabilities of CEST MRI make it a promising target for *in vivo* imaging applications such as the diagnosis of stroke (16-20) as well as detection and grading of tumors (9,21-31).

CEST MRI often involves a series of images with saturation pulse sweeping over a range of frequency offsets, with the signal changes along the extracted offset, also termed as Z-spectra (32). The most commonly used CEST quantification method, namely, MT ratio asymmetry (MTR_{asym}) analysis (33), takes the difference between two CEST images at opposite frequency offsets ($\pm\Delta\omega$) as

$$MTR_{asym} = \frac{S_{sat}(-\Delta\omega) - S_{sat}(\Delta\omega)}{S_0} \quad [1]$$

where $S_{sat}(-\Delta\omega)$ and $S_{sat}(\Delta\omega)$ are signals with saturated RF irradiation, which applied at the reference frequency and labeled proton frequency; S_0 is the reference signal without RF irradiation. MTR_{asym} is simple and easy to be calculated, which has been shown to correlate with tumor grade in case of amide proton transfer (APT) (34-36). However, MTR_{asym} is susceptible to several types of contamination, including B_0 inhomogeneity (37), direct saturation (DS) and semisolid macromolecular magnetization transfer (MT). Moreover, it is incapable to separate nuclear overhauser effect (NOE) at resonance frequencies up field of water based on CEST contrast.

To further improve CEST specificity and its signal quantification, Z-spectra fitting has been employed to distinguish the contributions from multiple origins (38). Theoretically, the enhancement of CEST through Z-spectra is dependent on the pool size, exchange rate and relaxation

time (25,34), as demonstrated by Bloch-McConnell equations. However, the complex Bloch fitting strongly relies on the initialization and boundaries of fitting parameters (39). According to the shape of Z-spectra, other quantification methods have been proposed, including multiple-pool Lorentzian fitting (7,24,38-40) and Lorentzian difference (LD) analysis (18,40-42). Multiple-pool Lorentzian fits each 'dip' in Z-spectra using a Lorentzian shape, in which the reference signals can be obtained by setting the fitted amplitude of the target CEST or NOE pools to zero. However, multiple-pool Lorentzian fitting requires the Z-spectra to be collected at a sufficient sampling frequency, and thus such method is time consuming. In addition, it has different fitting parameters, and is sensitive to the signal-to-noise ratio of Z-spectra. Besides, the LD method is a simplified method that employs a single Lorentzian line as a reference to describe the DS and takes account of difference against experimental data for quantifying CEST and NOE signal. LD can be an easy and robust quantification method, especially at low $B_{1,sat}$ ($\leq 1 \mu T$ at 9.4 Tesla) (40), which has been initially validated in patients with stroke (18,40-42). However, LD analysis possesses the disadvantage of overestimating contributions from CEST and NOE effects (40). In particular, for fast-exchanging species that require higher $B_{1,sat}$, or for tissue with a strong MT contrast, the Z-spectra exhibit non-Lorentzian line-shape (40) making the results of LD analysis invalid. More importantly, the Z-spectrum appears more like a Gaussian line-shape, rather than a Lorentzian line-shape, when $B_{1,sat}$ is higher or in the presence of strong MT contrast (20,43).

During NMR spectroscopy analysis, Voigt spectra line profile is often defined by the convolution of Lorentzian and Gaussian terms (44-46). As an excellent approximation to Voigt profile, Pseudo Voigt profile is best defined as the weighted sum of Gaussian and Lorentzian (47). In this study, a Voxel-wise Optimization Pseudo Voigt Profile (VOPVP) fitting algorithm was developed to improve the reliability of *in vivo* CEST MRI quantification. To further compensate for the different levels of MT and DS, a $B_{1,sat}$ -dependent optimization was adopted into the VOPVP fitting based on the 5-pool Bloch simulations under different $B_{1,sat}$. To evaluate the performance of VOPVP

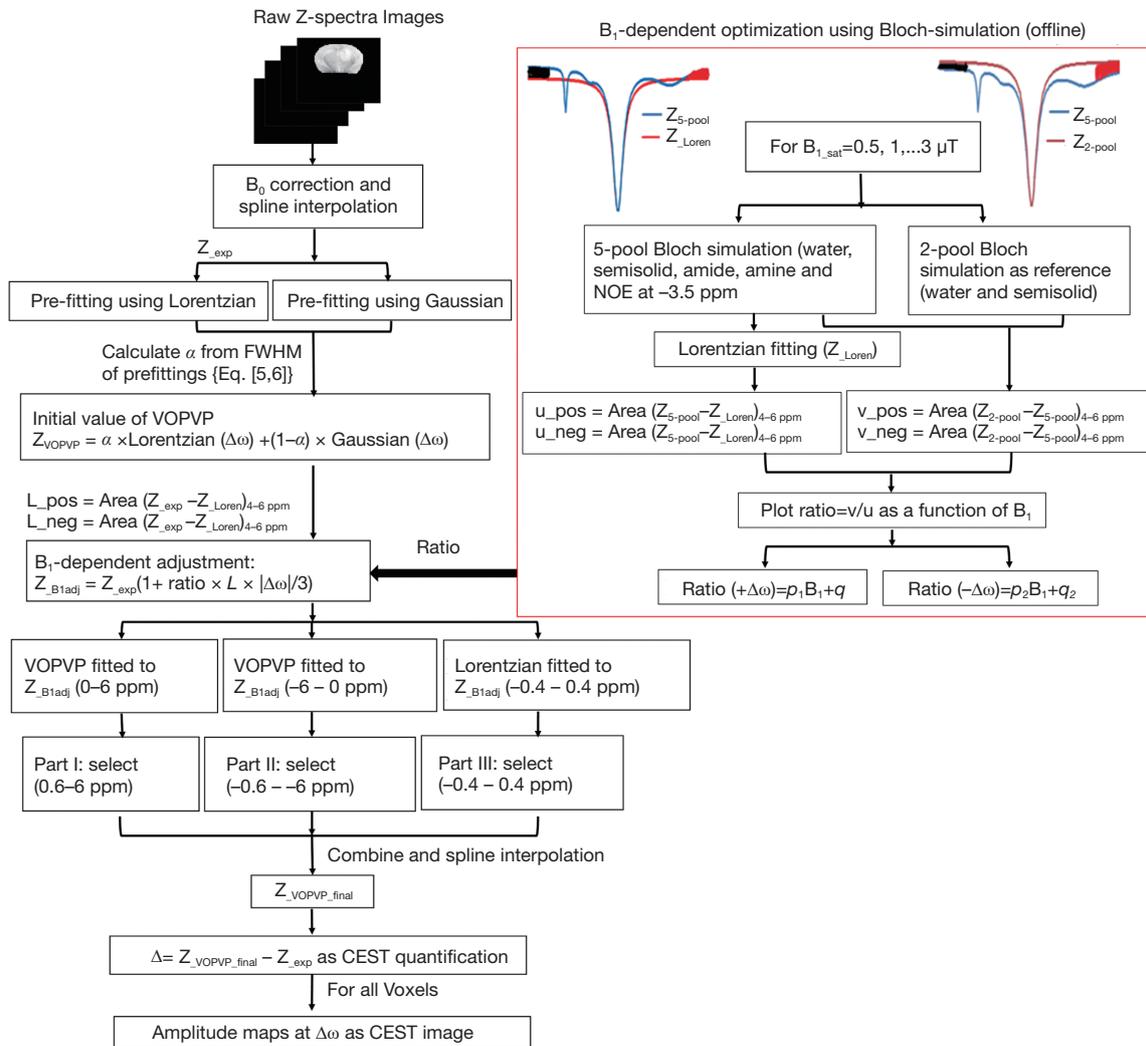


Figure 1 Flow chart of data processing steps of Voxel-wise Optimization Pseudo Voigt Profile (VOPVP) fitting approach.

fitting, an extensive Bloch-simulations was performed using previously published parameters (i.e., 5-pool model and 6-pool model with greater MT contributions) at various B_{1_sat} . The conventional LD and an analytical standard were also assessed and compared. Finally, an initial validation for *in vivo* application was carried out using a brain tumor-bearing mouse.

Methods

Theoretical concepts

The detailed flow of our VOPVP method is illustrated in *Figure 1*. The proposed fitted function, or termed as Pseudo

Voigt profile (47), was expressed by a weighted sum of Gaussian (G) and Lorentzian (L):

$$V(\Delta\omega) \approx \alpha \times L(\Delta\omega) + (1 - \alpha)G(\Delta\omega) \tag{2}$$

where α and $1-\alpha$ denote the proportionality coefficients of Lorentzian and Gaussian functions, respectively. The model function of Gaussian fitting can be described by

$$G(\Delta\omega) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(\omega_1 - \omega)^2}{2(\sigma)^2}} \tag{3}$$

where ω_1 is the frequency offset from the water resonance, while ω is the frequency offset of the CEST peak for the proton pool.

The model function of Lorentzian fitting can be given by

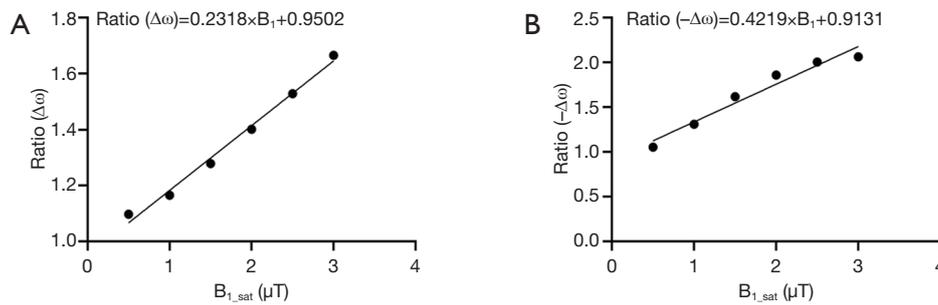


Figure 2 Relationship between (A) Ratio ($\Delta\omega$), (B) Ratio ($-\Delta\omega$), and B_{1_sat} .

$$L(\Delta\omega) = \frac{A}{\pi \left[1 + \frac{\omega_1 - \omega}{\sigma} \right]^2} \quad [4]$$

where ω_1 is the frequency offset from the water resonance, whereas A , ω and σ are the amplitude, frequency offset and linewidth of the CEST peak for the proton pool, respectively.

Thompson *et al.* (45) have proposed the following expression for the pseudo-Voigt approximation for the convolution of both Gaussian and Lorentzian functions, as presented by the full width at half maximum (FWHM) values of Gaussian and Lorentzian:

$$a = 1.36603 \left(\frac{\Gamma_L}{\Gamma} \right) - 0.47719 \left(\frac{\Gamma_L}{\Gamma} \right)^2 + 0.11116 \left(\frac{\Gamma_L}{\Gamma} \right)^3 \quad [5]$$

where

$$\Gamma = \left(\Gamma_G^5 + 2.69269 \Gamma_G^4 \Gamma_L + 2.42843 \Gamma_G^3 \Gamma_L^2 + 4.47163 \Gamma_G^2 \Gamma_L^3 + 0.07842 \Gamma_G \Gamma_L^4 + \Gamma_L^5 \right)^{1/5} \quad [6]$$

where Γ_G and Γ_L are the FWHM of Gaussian and Lorentzian, respectively.

VOPVP fitting

Figure 1 shows the flow chart of the proposed VOPVP fitting algorithm. Firstly, for the raw Z-spectra data, WASSR was performed to correct B_0 inhomogeneity. The obtained Z-spectra is labeled as Z_{-exp} . Gaussian and Lorentzian model pre-fitting was performed for Z_{-exp} in order to achieve the Lorentzian proportionality coefficient (a), based on the FWHM of Gaussian and Lorentzian derived from Eqs. [5] and [6], respectively. Subsequently, the area values of Z_{-loren} under Z_{-exp} between 4 and 6 ppm and between -4 and -6 ppm are named as L_{pos} and L_{neg} , respectively.

To further compensate for the line-shape changes under different B_{1_sat} 's, a B_1 -dependent adjustment was applied to the experimental Z-spectra (Z_{-exp}) according to the prior knowledge learned from 5-pool Bloch equation-based simulations at a range of B_{1_sat} 's. Simulated Z-spectra (Z_{5-pool}) of brain tissue with $B_0 = 9.4$ T were obtained through 5-pool Bloch equation-based simulations (48), for a range of B_{1_sat} (0.5, 1, 1.5, 2, 2.5 and 3 μ T). Accurate reference spectra describing DS and MT were determined using a 2-pool model (water and semisolid), with the residual with Z_{5-pool} for CEST quantification. The Lorentzian fitting was also performed. The residual areas with regarding to Z_{5-pool} , were calculated for Lorentzian fitting [u_{pos} (4 to 6 ppm) and u_{neg} (-4 to -6 ppm)], and also for the 2-pool model [v_{pos} (4 to 6 ppm) and v_{neg} (-4 to -6 ppm)]. Then, for each B_{1_sat} , the two ratios of $\Delta\omega$ and $-\Delta\omega$ were calculated as follows: (A) *Ratio* ($\Delta\omega$) = v_{pos} / u_{pos} . (B) *Ratio* ($-\Delta\omega$) = v_{neg} / u_{neg} . Figure 2 plotted *Ratio* ($\Delta\omega$) and *Ratio* ($-\Delta\omega$) as a function of B_{1_sat} . As seen, when $B_{1_sat} < 1$ μ T, ratio values are close to 1, indicating accurate quantification of LD. However, when $B_{1_sat} \geq 1$ μ T LD become inaccurate with ratio > 1 . For both *Ratio* ($\Delta\omega$) and *Ratio* ($-\Delta\omega$), a linear relationship with B_{1_sat} can be determined, providing the prior knowledge of fitting errors. Here, before starting VOPVP optimization, a B_1 -dependent adjustment was applied to Z_{-exp} , resulting in $Z_{B1adj} = Z_{-exp} (1 + Ratio \times L \times |\Delta\omega|/3)$. By multiplying Z_{-exp} with the Ratio values at the applied B_{1_sat} , the adjusted spectra (Z_{B1adj}) can compensate for the difference between LD and accurate quantification.

Then, with the initial value of VOPVP fitting defined by Eqs. [2-4], the fitting to Z_{B1adj} was divided into three parts. Part I, VOPVP function was used to fit the Z_{B1adj} between 0 and 6 ppm. Part II, VOPVP function was used to fit the Z_{B1adj} between -6 and 0 ppm. Part III, Lorentzian was employed to fit the Z_{B1adj} between -0.4 and 0.4 ppm. The final fitting results integrated the fitted data from part

Table 1 Parameters for the Bloch equation-based simulations (9.4T)

Parameters	Water	Amide (3.5 ppm)	Amine (2 ppm)	NOE (-3.5 ppm)	MT (-2.3 ppm)	NOE (-1.6 ppm)
5-pool (48)						
f_s	1	0.004	0.002	0.0033	0.04	-
$K_{sw} (s^{-1})$	-	30	1000	20	20	-
T_1 (s)	2.2	2.2	2.2	2.2	2.2	-
T_2 (ms)	36	36	36	0.4	20×10^{-3}	-
6-pool (40)						
f_s	1	0.0015	0.0003	0.007	0.1	0.003
$K_{sw} (s^{-1})$	-	50	500	50	25	50
T_1 (s)	1.5	1.5	1.5	1.5	1.5	1.5
T_2 (ms)	50	2	10	0.5	0.015	1

NOE, nuclear overhauser enhancement; MT, magnetization transfer.

I (0.6 to 6 ppm), part II (-6 to -0.6 ppm) and part III (-0.4 to 0.4 ppm). Then, Spline interpolation was used to assess the final fitting data, namely, Z_{VOPVP_final} . For all Voxels, the difference between Z_{VOPVP_final} and Z_{exp} was calculated to obtain the amplitude of maps at $\Delta\omega$. DS effects in weak range at both sides of 0 ppm with the line-shape similar to Lorentzian were fitted into the part III. The Z-spectra was far from 0 ppm and might contain MT components, which made Pseudo Voigt Profile an ideal fitting method. Moreover, there was no exchangeable proton within 0.6 ppm, according to the exchangeable proton chemical shifts for various diamagnetic agents (49) ranging from 0 to 7 ppm. Therefore, only the accuracy of fitting within ± 6 ppm was considered.

LD fitting

In addition, Lorentzian difference (LD) fitting (40,50) was carried out during the simulation. In this method, Lorentzian fitting was performed to evaluate the values of Z-spectra (-10 to -6.25 ppm, -1.7 to 1.7 ppm and 6.25 to 10 ppm at 9.4T), while spline interpolation was used to complete the entire fitting process. The fitted spectra were adopted as reference signals, representing the DS and semi-solid MT effects. The residual spectra of CEST (40) were formed by subtracting the measured Z-spectra from the fitted spectra.

For *in vivo* experiments, the offsets greater than ± 6 ppm were not collected due to the restriction of scanning time. To improve LD performance, a compensate strategy similar

to previous research (18) was employed, where the acquired Z-spectra were normalized by S_{sat} (-6 ppm) of the lower B_{1-sat} , and then fitted by Lorentzian fitting.

Simulation

To assess the performance of the proposed VOPVP method, Bloch equation-based simulations were carried out using both 5-pool exchange model (free water, amide, amine, MT and NOE at -3.5 ppm) (51) and 6-pool model (free water, amide, amine, MT, NOE at -3.5 ppm and NOE at -1.6 ppm) (40). Simulation parameters for rodent brain tissue at 9.4 Tesla are listed in *Table 1*. Specifically, the 6-pool model contained more MT and NOE components but less amides and amines in comparison with 5-pool model (40,48). To further evaluate the robustness of our method, simulations were performed at six different B_{1-sat} levels, i.e., 0.5, 1, 1.5, 2, 2.5 and 3 μ T.

To assess the robustness of our VOPVP method, we further performed simulation for a range of T_{1w} (0.5 to 2.5 s) and T_{2w} (25 to 125 ms), all using the same ratio values. To prove the feasibility at clinical field strengths, the ratios were calculated (*Figure S1*) using the parameters at 3T for rodent brain tissue (*Table S1*). Then the VOPVP fittings were performed and compared, using either ratios calculated from 3T, or those from 9.4T.

In vivo experiment

Animal experiments were performed in accordance with the guidelines of Johns Hopkins University Animal Care and

Use Committee guidelines. Balb/c NOD/SCID mouse were xenografted intracranially with 100,000 human glioblastoma cells to striatum of the brain (52,53) with MR imaging performed 6-week post-injection. *In vivo* MRI experiments were conducted on an 11.7T horizontal bore scanner (Bruker Biospec, Germany) using a transmit-receiver volume coil (23 mm diameter). CEST MRI images were acquired using a continuous wave pre-saturation pulse ($T_{\text{sat}}=2,500$ ms), followed by a rapid acquisition with relaxation enhancement (RARE) readout (RARE factor =12). B_0 inhomogeneity was then corrected using WASSR (54). The Z-spectra were acquired from -6 to 6 ppm with an interval of 0.25 ppm at three $B_{1\text{-sat}}$ of 0.8, 1.2 and 2.4 μT . The other parameters were as follows: TR/TE =5,500 ms/11 ms, slice thickness =1 mm, FOV =17×14 mm² and matrix size =96×64.

Evaluation criteria

The obtained data were evaluated by four parameters: (I) the sum of squares due to error (SSE), (II) coefficient of (R-square) determination (39), (III) simple analytic solution to the apparent exchanged-dependent relaxation (AREX) (20,23,51,55,56), and (IV) contrast-to-noise ratio (CNR) for *in vivo* experiments (39). The AREX was further defined as follows:

To evaluate the accuracy of CEST quantification methods in numerical simulations, we used $R_{\text{ex}}^{\text{CEST}}(\Delta\omega)$ (20,40,55,57) as a gold standard, which is independent of non-specific tissue parameters such as T_{1w} , DS and semi-solid MT effects:

$$R_{\text{ex}}^{\text{CEST}}(\Delta\omega) = \frac{f_s k_{\text{sw}} \omega_1^2}{\omega_1^2 + (R_{2s} + k_{\text{sw}})k_{\text{sw}} + (\Delta\omega - \Delta)^2 k_{\text{sw}} / (R_{2s} + k_{\text{sw}})} \quad [7]$$

where f_s is solute concentration, k_{sw} is solute-water exchange rate, R_{2s} is solute transverse relaxation and ω_1 is irradiation power. In comparison with $R_{\text{ex}}^{\text{CEST}}(\Delta\omega)$, AREX, the inverse metric of the Z-spectra fitted by LD and VOPVP, was defined as below (40,55):

$$\text{AREX}(\Delta\omega) = \left(\frac{1}{Z_{\text{lab}}(\Delta\omega)} - \frac{1}{Z_{\text{ref}}(\Delta\omega)} \right) R_{\text{obs}}(1 + f_c) \quad [8]$$

where f_c is semi-solid MT pool size ratio.

Results

Simulations

Figure 3 displays the simulated Z-spectra, VOPVP fitting

and LD fitting of $B_{1\text{-sat}}$ at 0.5, 1, 1.5, 2, 2.5 and 3 μT , apart from the difference between VOPVP and the simulated data. For the simulated data through 5-pool model, the difference spectra generated by VOPVP and Lorentzian fitting could reveal the peaks arising from amide proton at 3.5 ppm, amine protons at 2 ppm and NOE at -3.5 ppm (NOE at -1.6 ppm for 6-pool only). However, LD overestimated the amide, amine CEST signals when $B_{1\text{-sat}}=1, 1.5$ and 2 μT , while underestimated NOE when $B_{1\text{-sat}}=2.5$ and 3 μT . In contrast, for all the saturation powers, our VOPVP method could provide a closer fitting to the non-specific parts of Z-spectra (-6 to -5 ppm, -1.5 to 1.5 ppm and 4 to 6 ppm), as quantitatively indicated by both SSE and R-square (Table 2). As aforementioned, the 6-pool model may contain more MT and NOE components but less amides and amines than the 5-pool model. Our results showed the SSE of 6-pool increased by up to 100% from 5-pool model (Table 2) ($B_{1\text{-sat}}=3$ μT) is not only NOE at -1.6 ppm but also the 6-pool model containing more MT components.

In addition, the AREX metrics derived from VOPVP fitting and LD fitting were further compared with $R_{\text{ex}}^{\text{CEST}}$ analytical standard (Figure 4 and Table 3). For the 6-pool model, LD overestimated all the CEST and NOE signals. For the 5-pool model, LD overestimated amides and NOE (3.5 ppm) at $B_{1\text{-sat}} \leq 2$ μT (1, 1.5 and 2 μT), while underestimated APT and NOE (3.5 ppm) at 3 μT . For both the 5-pool and the 6-pool models, the derived $\text{AREX}_{\text{VOPVP}}$ spectra were significantly closer to the standard $R_{\text{ex}}^{\text{CEST}}$ spectra, especially at $B_{1\text{-sat}} \geq 1$ μT (1, 1.5, 2, 2.5 and 3 μT). Table 3 lists the ratios of the peak intensities of the AREX_{LD} and $\text{AREX}_{\text{VOPVP}}$ metrics to those of $R_{\text{ex}}^{\text{CEST}}$. Notably, for the 5-pool model, $\text{AREX}_{\text{VOPVP}}$ at amide frequency (3.5 ppm) and NOE (-3.5 ppm) were relatively close to $R_{\text{ex}}^{\text{CEST}}$ at all $B_{1\text{-sat}}$. While for the 6-pool model with a greater MT contribution, $\text{AREX}_{\text{VOPVP}}$ could estimate $R_{\text{ex}}^{\text{CEST}}$ more accurately at lower $B_{1\text{-sat}}$ (≤ 2 μT), but still underestimated the APT at 2.5 and 3 μT ; Nevertheless, for all cases, $\text{AREX}_{\text{VOPVP}}$ outperformed AREX_{LD} with regard to all peaks (i.e., APT, amine and NOE).

The fitted linear function at 3T (Figure S1) suggested a slightly different slope and shift compared with those calculated at 9.4T (Figure 2). As seen, $\text{AREX}_{\text{VOPVP}}$ values were closer to the analytical solution $R_{\text{ex}}^{\text{CEST}}$ than AREX_{LD} values, for both $B_{1\text{-sat}}=1$ μT and $B_{1\text{-sat}}=2$ μT (Figure 5). As seen, the two kinds of VOPVP fitting curves are almost identical, which both resulted in accurate quantification ($\text{AREX}_{\text{VOPVP}}$) compared with the analytical standard $R_{\text{ex}}^{\text{CEST}}$.

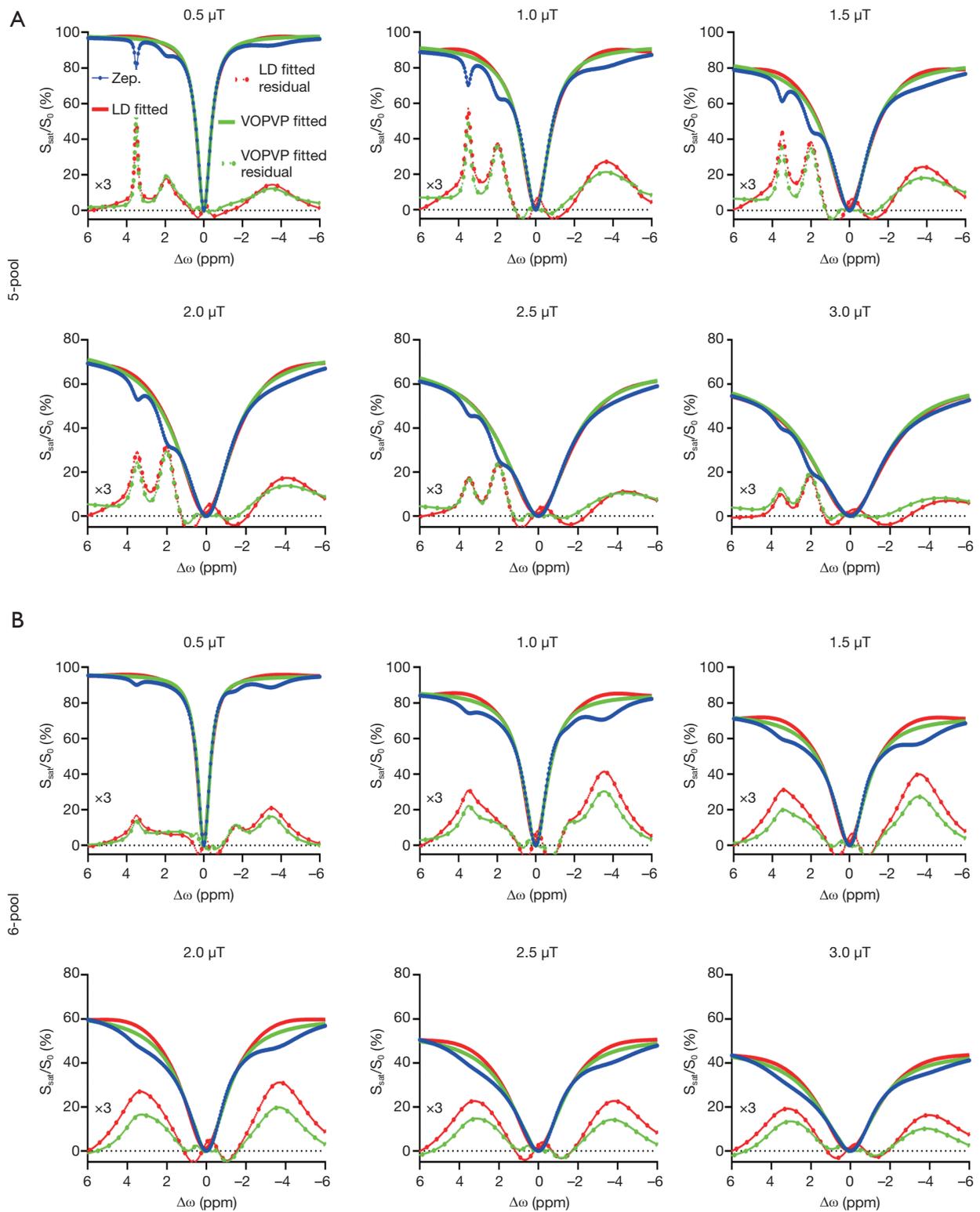


Figure 3 Comparison of VOPVP fitting and LD fitting using simulating Z-spectra, for B_{1_sat} of 0.5, 1, 1.5, 2, 2.5 and 3 μT , respectively. (A) The 5-pool Bloch-simulation; (B) the 6-pool Bloch-simulation.

Table 2 Comparison of fitting quality of LD and VOPVP in simulation

Number of pools	Quantification quality	B_{1_sat} (μ T)	0.5	1	1.5	2	2.5	3
5	SSE	LD	0.1101	0.4247	0.3793	0.2085	0.0946	0.0403
		VOPVP	0.0365	0.1355	0.1202	0.0744	0.0498	0.0332
	R-square	LD	0.9865	0.9479	0.9535	0.9744	0.9884	0.9951
		VOPVP	0.9955	0.9834	0.9853	0.9905	0.9951	0.9959
6	SSE	LD	0.1359	0.5682	0.5633	0.3545	0.1907	0.0967
		VOPVP	0.0155	0.0309	0.0305	0.0196	0.0157	0.012
	R-square	LD	0.9195	0.6636	0.6665	0.7901	0.8871	0.9427
		VOPVP	0.9908	0.9817	0.9821	0.9884	0.9907	0.9928

LD, Lorentzian difference; VOPVP, Voxel-wise Optimization of Pseudo Voigt Profile; SSE, sum of squares due to error.

(Figure S2, Table S2).

Tumor mouse

Further, VOPVP fitting was applied to quantify the contributions of APT, glutamate, amine and NOE effects in a mouse bearing glioblastoma. The T_2w image (Figure 6A) indicated the anatomy, with a tumor ROI and the contralateral control one marked. To visualize the quantified spectra for all voxels, the offset-cut images were plotted with the residual spectra of LD fitting and VOPVP (Figure 6B,C). Transverse coordinates between 56 and 66 are the location of the tumor. Notably, the offset-cut values of VOPVP fitting were significantly higher at 3.5 ppm and 2 ppm in tumor than those in normal contralateral tissue. In contrast, the offset-cut values of LD fitting were significantly higher for Amide 3.5 ppm, Glu-CEST 3 ppm, Guanidinium-Amine 2 ppm and lower for NOE between -2 and -5 ppm in the tumor than those in normal contralateral tissue. The differences between VOPVP fitting and LD fitting for tumor ROI and normal contralateral ROI at three B_{1_sat} level (0.8, 1.2 and 2.4 μ T) are presented in Figure 6D,E. Moreover, the dips centered at -3.5, 2 and 3.5 ppm could be clearly observed on the Z-spectra at relatively low B_{1_sat} , which corresponded to aliphatic NOE, guanidine amine and amide, respectively. Another dip around -1.6 ppm was observed in normal tissues, but not in tumors with low B_{1_sat} , which were consistent with previous reports (58,59). Theoretically, a dip at 3 ppm from Glu-CEST should be visible at high B_{1_sat} (10). However, it was not obviously shown on the Z-spectra due to the broadened dips. The residual of both VOPVP and LD fitting for the

ROIs of tumor and normal contralateral tissue appeared at 3.5 ppm (amide), downfield from water and 2–5 ppm (NOE) up field from water. Overall, the fitting curves of VOPVP for the two ROIs were closer to the experimental measurements compared to those obtained by LD. Besides, the overestimation of LD fitting becomes obvious with the increasing B_{1_sat} , which was also observed in a recent CEST study of simulations at 9.4T (40). The peaks appeared at 2 ppm could be clearly observed on the MTR_{asym} map (Figure 6F) at all B_{1_sat} , which were consistent with the conclusion drawn from the fitted residual spectra.

Furthermore, the proposed VOPVP method was evaluated by comparing with LD fitting and MTR_{asym} (3.5 ppm) (Figure 7). Figure 7 shows the fitted amplitude maps using MTR_{asym} at 3.5 ppm, LD fitting and VOPVP fitting in a mouse tumor model. The images were fitted voxel-wise to Eq. [2] by using the nonlinear fitting function (lsqcurvefit) in MATLAB. In line with previous findings on the APT imaging of glioma (4,60–62), a remarkably higher APT effect was found in tumors fitted by VOPVP. For NOE (VOPVP fitting), our results demonstrated the intensity of tumor was increased at higher B_{1_sat} (1.2 and 2.4 μ T) compared to normal tissue, but decreased at lower B_{1_sat} (0.8 μ T). Moreover, VOPVP fitting revealed a pronounced positive contrast in the tumor analyzed by Glu-CEST map. Whilst, the NOE (LD fitting) in tumor was lower than that in normal tissue at $B_{1_sat} = 0.8 \mu$ T, which were consistent with previous findings (63). Additionally, MTR_{asym} (3.5 ppm) indicated that the signal intensity of tumor location was significantly higher than that of normal contralateral tissue location, which was in accordance with the results of previous studies (4,63,64).

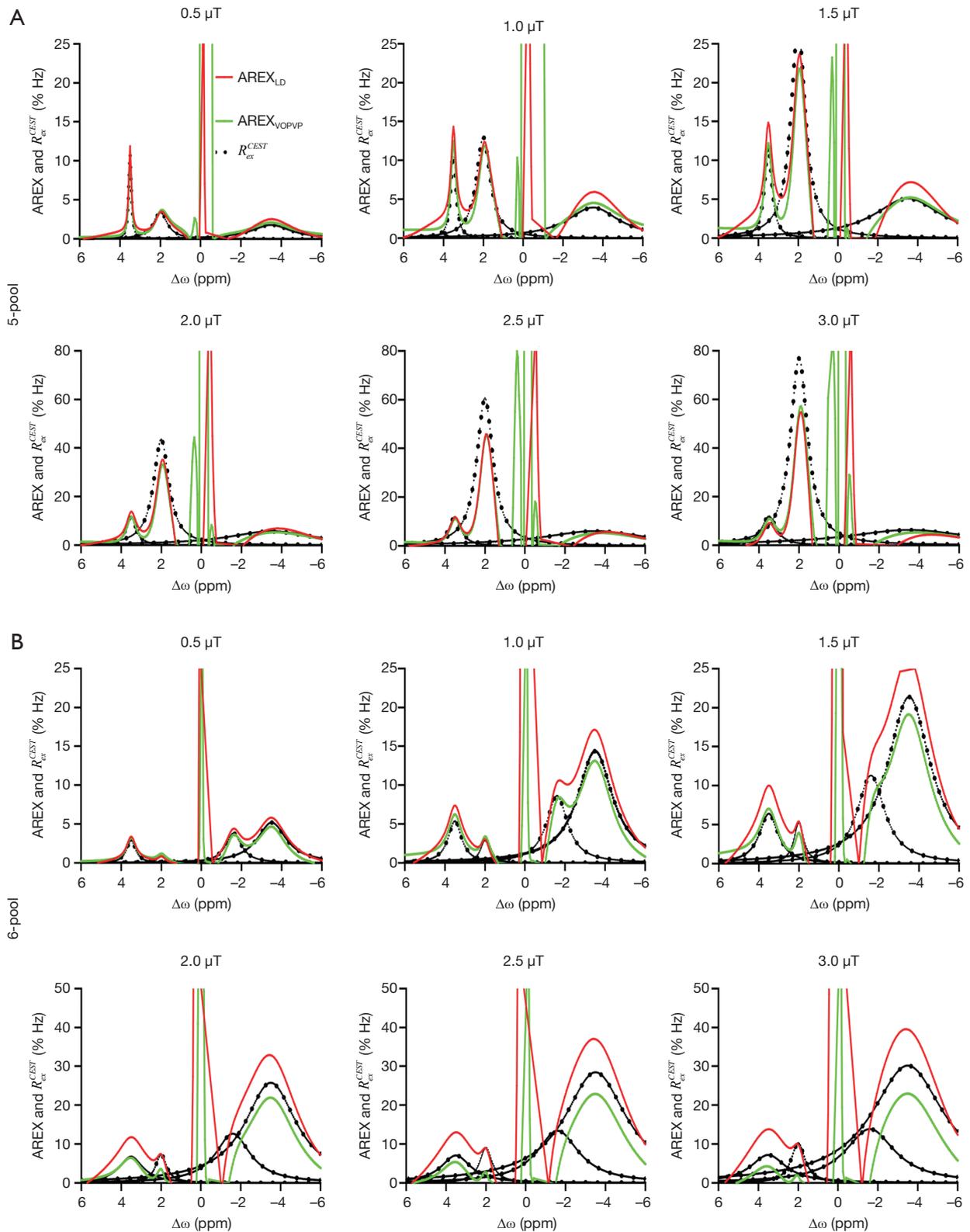


Figure 4 Quantification of the fitted Z-spectra using AREX (AREX_{LD} and AREX_{VOPVP}), and comparison with the analytical R_{ex}^{CEST} spectra, for B_{1_sat} of 0.5, 1, 1.5, 2, 2.5 and 3 μT , respectively. (A) The 5-pool Bloch-simulation; (B) the 6-pool Bloch-simulation.

Table 3 Comparison of quantified peaks using LD and VOPVP with the analytical R_{ex}^{CEST} as a gold standard (40)

Variable	Amide	Intermediate exchanging amine	NOE (-1.6 ppm)	NOE (-3.5 ppm)
$AREX_{LD}/R_{ex}^{CEST}$ (5-pool)	1.1, 1.2, 1.3, 1.2, 1.0, 0.8	1.0, 0.9, 0.9, 0.8, 0.7, 0.7	–	1.4, 1.5, 1.4, 1.2, 0.8, 0.4
$AREX_{VOPVP}/R_{ex}^{CEST}$ (5-pool)	1.0, 1.0, 1.0, 1.0, 0.9, 0.9	1.0, 0.9, 0.8, 0.7, 0.7, 0.7	–	1.1, 1.1, 1.0, 1.0, 1.0, 1.0
$AREX_{LD}/R_{ex}^{CEST}$ (6-pool)	1.8, 2.3, 2.7, 2.9, 3.0, 3.0	2.8, 2.6, 2.4, 2.2, 2.1, 2.0	1.4, 1.5, 1.6, 1.7, 1.8, 1.8	1.5, 1.5, 1.5, 1.6, 1.6, 1.6
$AREX_{VOPVP}/R_{ex}^{CEST}$ (6-pool)	1.1, 1.1, 1.1, 0.9, 0.8, 0.6	1.4, 1.2, 0.8, 0.5, 0.3, 0.2	0.9, 1.0, 0.6, 0.4, 0.2, 0.1	0.8, 0.9, 0.9, 1.0, 1.0, 1.0

B_{1-sat} = 0.5, 1, 1.5, 2, 2.5, 3 μ T. AREX, apparent exchanged-dependent relaxation; LD, Lorentzian difference; VOPVP, Voxel-wise Optimization of Pseudo Voigt Profile.

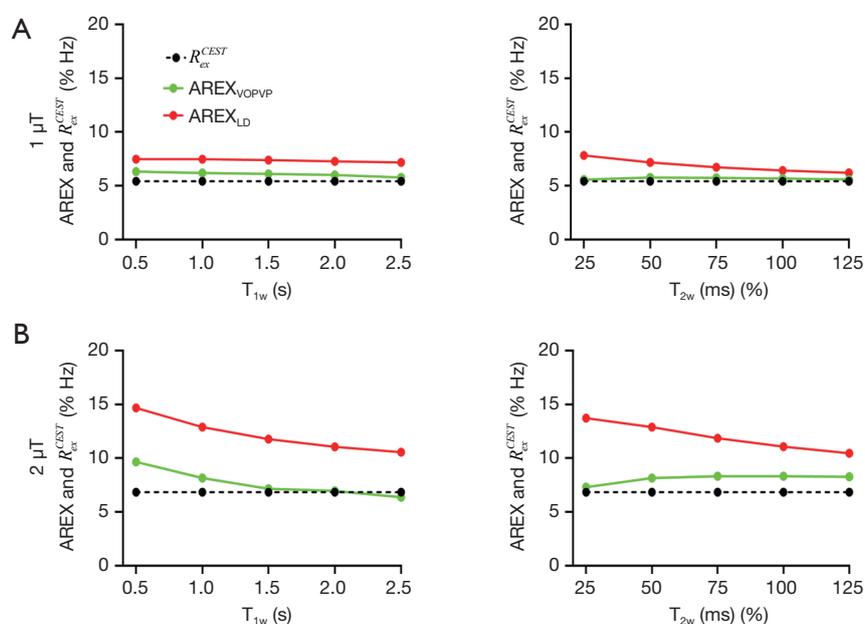


Figure 5 $AREX_{LD}$, $AREX_{VOPVP}$ and calculated R_{ex}^{CEST} for APT from simulated Z-spectra with variation of T_{1w} and T_{2w} , with the B_{1-sat} of (A) 1 μ T, (B) 2 μ T.

Table 4 describes the quality of each CEST map. For APT and Glu-CEST, VOPVP method exhibited higher CNR than LD method and MTR_{asym} (3.5 ppm), when B_{1-sat} > 1 μ T.

Discussion

In this study, we propose a novel CEST quantification method, namely VOPVP, by fitting Z-spectra with a linear combination of Gaussian- and Lorentzian-line shapes as the reference spectra and taking the difference among experimental data for CEST quantification. To improve the conventional LD and enhance its robustness for various

occasions (e.g., larger B_{1-sat} and greater MT), we not only modified the fitting function from Lorentzian to Pseudo Voigt Profile (PVP), but also integrated a B_1 -dependent optimization for better compensation of the altered DS (spillover effect) and MT under different B_{1-sat} . The main purposes of Z-spectra fitting in Lorentzian and VOPVP are to generate a reference spectrum without CEST and NOE, and to best simulate the confounding MT and DS. The semisolid MT effect is asymmetric around the water peak, which induces signal decline over a wide frequency range. It has been reported that a baseline term against the Lorentzian analysis can minimize the impact of global MT effect and noise arising from motion (40,50). A previous

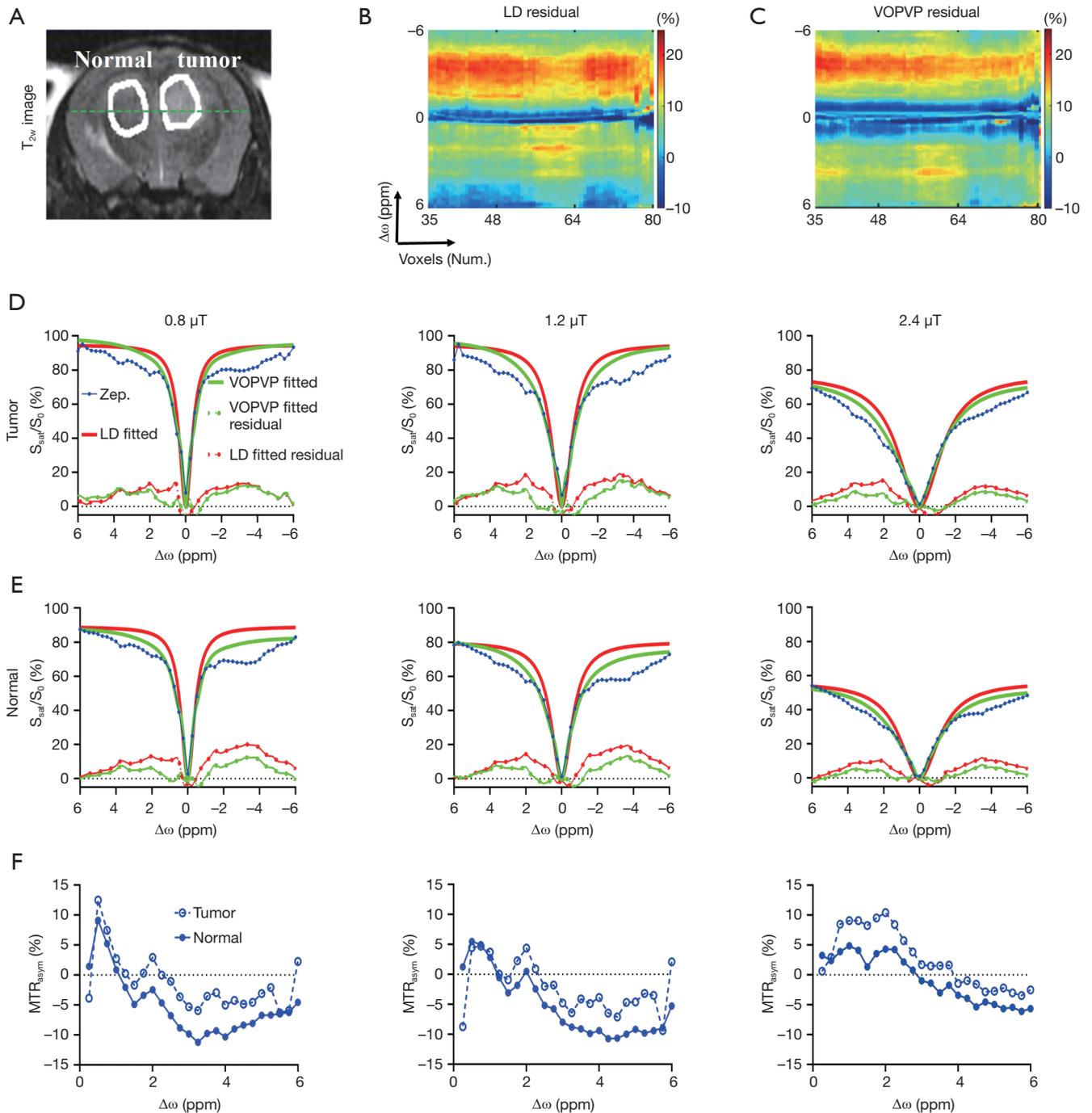


Figure 6 Quantitative assessment of *in vivo* tumor-bearing mouse brain. (A) The T_{2w} image, marked with a tumor ROI and the contralateral control for spectral analysis. (B) The offset-cut map using residual spectra of LD fitting for $B1_{\text{sat}} = 1.2 \mu\text{T}$, which locations are indicated by dash line in (A) of T_{2w} image. (C) The offset-cut map using residual spectra of VOPVP for $B1_{\text{sat}} = 1.2 \mu\text{T}$, which locations are indicated by dash line in (A) of T_{2w} image. (D) Comparison of VOPVP fitting and LD fitting for tumor region. (E) Comparison of VOPVP fitting and LD fitting for the normal contralateral region. (F) MTR_{asym} analysis both for the tumor region and the normal contralateral region. VOPVP, Voxel-wise Optimization of Pseudo Voigt Profile; LD, Lorentzian difference; MTR_{asym} , magnetization transfer ratio asymmetry.

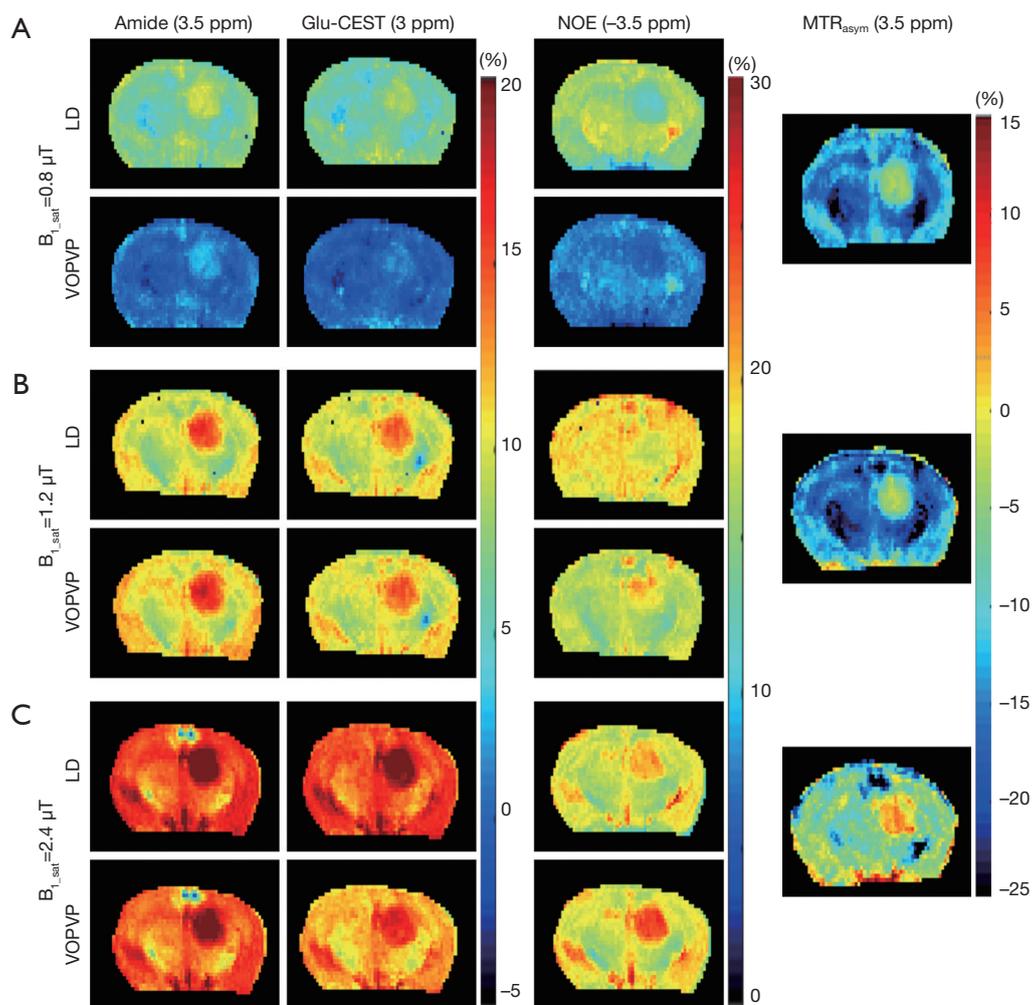


Figure 7 Comparison of fitted amplitudes maps using VOPVP fitting, Voxel-wise LD fitting and MTR_{asym} (3.5 ppm) in a representative mouse brain, for $B_{1_{\text{sat}}}$ of (A) 0.8 μT , (B) 1.2 μT and (C) 2.4 μT . VOPVP, Voxel-wise Optimization of Pseudo Voigt Profile; LD, Lorentzian difference; MTR_{asym} , magnetization transfer ratio asymmetry.

study has renormalized CEST Z-spectra by averaging the signal intensity of both end of Z-spectra of at relatively lower $B_{1_{\text{sat}}}$ (18) before performing LD fitting. Similarly, in our VOPVP method, a compensate ratio factor was applied to the experimental Z-spectra data, according to the acquisition $B_{1_{\text{sat}}}$. The relationship between the ratio and $B_{1_{\text{sat}}}$ was established in advance through an offline step using the 5-pool Bloch simulation (Figures 1,2). Both simulation and *in vivo* mouse revealed that VOPVP displayed a better approximation to the referenced part of Z-spectra in comparison with LD analysis. Despite that VOPVP outperformed the conventional LD when the acquisition $B_{1_{\text{sat}}}$ is larger for fast-exchangeable species or when the tissue imposes a greater MT contribution, this

method does not work well with larger $B_{1_{\text{sat}}}$ and greater MT component, especially not appropriate for amines and NOE (-1.6 ppm) that are closer to water (Table 3).

In the proposed approach we applied a B1-dependent adjustment to the measured Z-spectra, before starting of the optimization of pseudo voigt profile. The equation for adjustment was obtained offline, through simulations using a previously-published 5-pool model for brain tissue at 9.4T. Accurate reference spectra describing DS and MT were determined using a 2-pool model (water and semisolid), while Lorentzian fitting was also performed. The inaccuracy of LD fitting was further defined by the ratio of two residual areas, corresponding to the Lorentzian fitting spectrum and the accurate reference spectrum. As seen in Figure 2,

Table 4 Comparison of CNR between MTR_{asym} (3.5 ppm), LD fitting and VOPVP fitting in tumor mouse brain at 11.7T

$B_{1\text{-sat}}$ (μT)	MTR_{asym} (3.5 ppm)	Fitting method	APT (3.5 ppm)	Glu-CEST (3 ppm)	NOE (3.5 ppm)
0.8	3.46	LD	2.95	2.12	3.31
		VOPVP	3.10	2.30	3.18
1.2	2.01	LD	1.12	0.71	0.94
		VOPVP	2.42	2.16	2.42
2.4	2.89	LD	3.08	1.82	1.71
		VOPVP	5.65	4.91	5.65

CNR, contrast-to-noise ratio; MTR_{asym} , magnetization transfer ratio asymmetry; LD, Lorentzian difference; VOPVP, Voxel-wise Optimization of Pseudo Voigt Profile; APT, amide proton transfer; CEST, chemical exchange saturation transfer; NOE, nuclear overhauser enhancement.

when $B_{1\text{-sat}} < 1 \mu\text{T}$, the ratio is close to 1, indicating accurate quantification of LD. But, for larger $B_{1\text{-sat}}$, LD inaccurately quantified CEST signal with ratio > 1 . We also figured the linear relationships between ratios and $B_{1\text{-sat}}$. This prior knowledge of inaccuracy of LD at different $B_{1\text{-sat}}$, was then employed in the online optimization step, to produce an adjusted Z-spectra better representing the DS and MT contributions under applied $B_{1\text{-sat}}$. In another word, our quantification approach employed the prior knowledge of LD mismatch at different $B_{1\text{-sat}}$ to constrain the optimization algorithm (Levenberg-Marquardt algorithm here), leading to more accurate quantification. Despite that the adjustment uses Ratios that calculated from a 5-pool model of brain tissue, the followed VOPVP optimization will make it work for a range of tissue parameters (T_{1w} and T_{2w}), as shown in *Figures 3,4,5*. The Ratios is also applicable for different filed strengths, as validated by the 3T simulations (*Figures S1,S2, Table S1*). This constrained optimization method, through learning from the off-line simulations, could also applied to other fitting methods for CEST MRI in future.

Apart from taking the difference between a fitting reference spectra and the experimental data, several other quantification methods have been proposed, including apparent exchange-dependent relaxation (AREX) (5), extrapolated semi-solid magnetization transfer reference (EMR) (4,65), multi-pool Bloch-McConnell (BM) fitting (32), three-offset approach (23,66) and the combination of these quantitative methods (20,23,35,51). Superior to MTR_{asym} , all these methods allow the separation of CEST and NOE effect. However, the accuracy and robustness of these methods are varied, and each has its own limitations. For instance, AREX has been applied only to slow- (e.g., APT) (27,38) and intermediate-exchangeable [e.g., creatine (creCEST) (67)] solutes, which is also a

fitting approach to quantify fast-exchangeable amine CEST signals (5,27). BM fitting requires prior knowledge of parameters (e.g., T_2 and k_{ex} of each exchanging proton) and is time consuming compared to LD fitting and AREX (68). EMR approach has the potential to be an important and accurate CEST MRI quantitative technique (4), but it may overestimate the measurements of APT and NOE (4). Three-offset method is a relatively simple quantification approach (23,66). However, the linear assumption underlying the three-offset method may be oversimplified (39,40).

NOEs are depended on the applied $B_{1\text{-sat}}$ and filed strength. It has been reported there is no significant difference in the NOE (9.4T, 1 μT) between tumors and normal contralateral tissues (23). Previous findings have shown that the NOE signal at 4.7 Tesla in tumor is lower than that in normal contralateral tissue (63), which are consistent with the results of offset-cuts (*Figure 6B,C*). APT imaging, a specific form of CEST, can potentially serve as a non-invasive means to characterize abnormal tissues such as tumors (23). Previous reports have shown that the APT-related pool size of the tumor center and rim is significantly larger than that of normal tissue, as opposed to the NOE-related pool size. Moreover, APT can detect malignant tumors (63,64,69), the changes that have been induced by elevated mobile cellular and peptide contents (70). In the present study, it can be seen that the intensity of APT signal is higher in tumor than in normal contralateral tissue, as revealed the offset-cuts (*Figure 6B,C*) and fitted amplitudes maps (*Figure 7*) of our proposed VOPVP fitting, which is consistent with the findings of previous literature (4,70).

As an improvement of LD method, our VOPVP fitting may provide a simple, robust and more accurate approach for quantifying CEST and NOE contrast. More *in vivo* validations and at the clinical field strength will be performed

in the future.

Acknowledgments

The authors would like to thank Dr. Chengyan Chu and Dr. Piotr Walczak at Johns Hopkins University for their generous offering of a tumor-bearing mouse.

Funding: This work was supported by the National Natural Science Foundation of China under Grant No.61601364, Xi'an Key Laboratory of Radiomics and Intelligent Perception Grant 201805060ZD11CG44, and by the Postgraduate Independent Innovation Project of Northwest University (China) Grant YZZ17180. *In vivo* MRI data of the mouse were collected under support of Johns Hopkins Radiology Britestar Award to Dr. Xiaolei Song.

Footnote

Conflicts of Interest: The authors have no conflicts of interest to declare.

Ethical Statement: MR imaging experiment on a tumor-bearing mouse was performed under the approval of the Johns Hopkins University Animal Care and Use Committee (ACUC) with protocol # MO13M251.

Disclaimer: The content is solely the responsibility of the author and does not necessarily represent the official views of the funding agencies.

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Cite this article as: Zhang L, Zhao Y, Chen Y, Bie C, Liang Y, He X, Song X. Voxel-wise Optimization of Pseudo Voigt Profile (VOPVP) for Z-spectra fitting in chemical exchange saturation transfer (CEST) MRI. *Quant Imaging Med Surg* 2019;9(10):1714-1730. doi: 10.21037/qims.2019.10.01

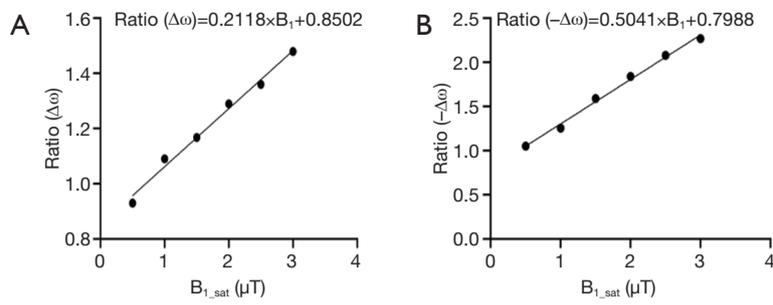


Figure S1 Relationship between (A) Ratio ($\Delta\omega$), (B) Ratio ($-\Delta\omega$), and B_{1_sat} at 3 T.

Table S1 Parameters for the Bloch Equation-Based simulations at 3T (5-pool) (48)

Parameters	Water	Amide (3.5 ppm)	Amine (2 ppm)	NOE (-3.5 ppm)	MT (0 ppm)
f_s	1	0.004	0.002	0.0033	0.04
$K_{sw} (s^{-1})$	–	30	1000	20	20
T_1 (s)	1.4	1.4	1.4	1.4	1.4
T_2 (ms)	100	50	50	0.4	20×10^{-3}

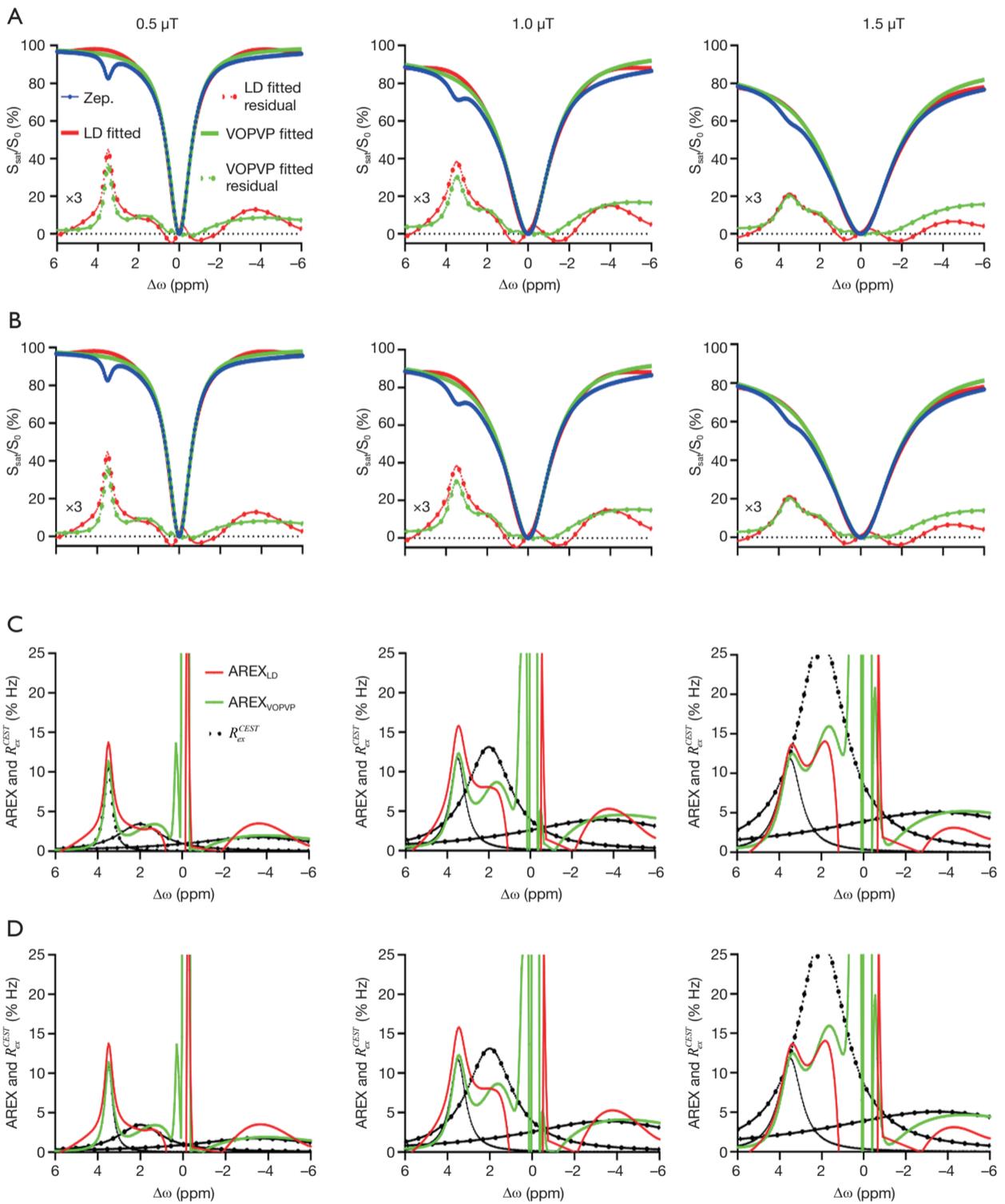


Figure S2 Quantitative assessment of simulation Z-spectra using ratios calculated from 3T. (A) Comparison of LD fitting and VOPVP fitting, which simulating Z-spectra using ratios calculated from 3T, for B_{1_sat} of 0.5, 1 and 1.5 μT . (B) Comparison of LD fitting and VOPVP fitting, which simulating Z-spectra using ratios calculated from 9.4 T, for B_{1_sat} of 0.5, 1 and 1.5 μT . (C) Quantification of the fitted Z-spectra using AREX ($AREX_{LD}$ and $AREX_{VOPVP}$, which using ratios calculated from 3 T, and comparison with the analytical R_{ex}^{CEST} spectra at 3 T, for B_{1_sat} of 0.5, 1 and 1.5 μT . (D) Quantification of the fitted Z-spectra using AREX ($AREX_{LD}$ and $AREX_{VOPVP}$, which using ratios calculated from 9.4 T, and comparison with the analytical R_{ex}^{CEST} spectra at 3 T, for B_{1_sat} of 0.5, 1 and 1.5 μT . LD, Lorentzian difference; VOPVP, Voxel-wise Optimization of Pseudo Voigt Profile; AREX, apparent exchanged-dependent relaxation.

Table S2 Comparison of quantified peaks using LD and VOPVP, which using ratios calculated from 3T and 9.4T, with the analytical R_{ex}^{CEST} as a gold standard at 3 T (40) (5-pool)

Variable	Amide (3.5 ppm)	Intermediate exchanging amine	NOE (-3.5 ppm)
$AREX_{LD}/R_{ex}^{CEST}$	1.2 1.3 1.1	0.8 0.6 0.5	2.0 1.3 0.5
$AREX_{VOPVP}/R_{ex}^{CEST}$ (using ratios calculated from 3T)	1.0 1.0 1.0	0.8 0.6 0.6	1.1 1.1 0.9
$AREX_{VOPVP}/R_{ex}^{CEST}$ (using ratios calculated from 9.4T)	1.0 1.0 1.0	0.8 0.6 0.6	1.0 1.0 0.9

AREX, apparent exchanged-dependent relaxation; LD, Lorentzian difference; VOPVP, Voxel-wise Optimization of Pseudo Voigt Profile; NOE, nuclear overhauser enhancement; CEST, chemical exchange saturation transfer.